Numerical Analysis of Approximate Deconvolution Models of Turbulence

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Abstract

If the NSE are averaged with a local, spacial, convolution type filter the resulting system is not closed due to the term g * (uu). A deconvolution operator G_N is one which satisfies:

$$u = G_N(g * u) + O(\delta^{2N+2}) \tag{0.1}$$

where δ is the filter width. This yields the closure method:

$$g * (uu) = g * (G_N(g * u)G_N(g * u)) + O(\delta^{2N+2})$$
(0.2)

We will review several solutions to the ill-possed deconvolution problem, present an "optimal" deconvolution procedure and present numerical analysis and numerical experiments with it.

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